

# Properties of MVD

$R = R_1 \bowtie R_2$  is written as  $X \twoheadrightarrow Y$  where  $X = R_1 \cap R_2$  and  $R_1 = X \cup Y$

- *Replication*: if  $X \rightarrow Y$  then  $X \twoheadrightarrow Y$
- *Coalescence*: If  $W \subset Y$  and  $Y \cap Z = \emptyset$  then  $X \twoheadrightarrow Y$  and  $Z \rightarrow W$  entails  $X \rightarrow W$
- *Reflexivity*:  $X \twoheadrightarrow X$
- *Augmentation*:  $X \twoheadrightarrow Y$  entails  $XZ \twoheadrightarrow YZ$
- *Additivity*:  $X \twoheadrightarrow Y$  and  $X \twoheadrightarrow Z$  entails  $X \twoheadrightarrow YZ$
- *Projectivity*:  $X \twoheadrightarrow Y$  and  $X \twoheadrightarrow Z$  entails  $X \twoheadrightarrow Y \cap Z$  and  $X \twoheadrightarrow Y-Z$
- *Transitivity*:  $X \twoheadrightarrow Y$  and  $X \twoheadrightarrow Z$  entails  $X \twoheadrightarrow Z-Y$
- *Pseudotransitivity*:  $X \twoheadrightarrow Y$  and  $YW \twoheadrightarrow Z$  entails  $XW \twoheadrightarrow Z-(YW)$
- *Complementation*:  $X \twoheadrightarrow Y$  entails  $X \twoheadrightarrow R-Y$  where  $R$  is the set of attributes of the schema