Golog+HTN^{TI}: Adding time and intervals to procedural and hierarchical control knowledge

Chitta Baral

Dept. of Computer Sc. & Eng. Arizona State University Tempe, AZ 85287, USA chitta@asu.edu Tran Cao Son Department of Computer Sc. New Mexico State University Las Cruces, NM 88003, USA

tson@cs.nmsu.edu

Le-Chi Tuan

Dept of Computer Sc. and Eng. Arizona State University Tempe, AZ 85287, USA lctuan@asu.edu

Abstract

In this paper we introduce a language for expressing procedural and HTN-based domain constraints. Our language starts with features from GOLOG and HTN and extends them so that we can deal with actions with duration by being able to specify time intervals between the start (or end) of an action (or a program) and the start of another action (or program). We then discuss a planner based on the answer set planning paradigm that can exploit such domain knowledge.

Introduction and Motivation

GOLOG (Levesque et al. 1997) is an Algol-like logic programming language for agent programming, and control and execution. It is based on a situation calculus theory of actions (Reiter 2000). GOLOG has been primarily used as a programming language for high-level agent control in dynamical environments (see e.g. (Burgard et al. 1998)). Although a planner can be written as a GOLOG program (See Chapter 10 of (Reiter 2000)), in (Son, Baral, & McIlraith 2001) an alternative view of GOLOG programs is presented. There it is viewed as an incompletely specified plan (or a form of procedural knowledge) that includes nondeterministic choice points that are £lled in by the planner. For example, the GOLOG program $a_1; a_2; (a_3|a_4|a_5); f$, when viewed as a procedural knowledge tells a planner that the first action of the plan should be a_1 , the second action should be a_2 , and the 3rd action should be one of a_3 , a_4 and a_5 such that f holds afterward. A planner, when given this procedural knowledge needs only to decide which one of a_3 , a_4 , or a_5 it should choose as its third action. In (Son, Baral, & McIlraith 2001) it is shown how such procedural knowledge can be exploited to speed up planning. There it is also shown how to combine constructs from HTN-planning with the GOLOG constructs.

Now suppose that actions have duration. In that case we may want to say that start a_1 and after 2 unit time of execution of a_1 start executing a_2 and so on. Similarly in an HTN-based domain constraint instead of the standard $a_1 \prec a_2$ – which means that a_1 should be executed before a_2 – we might want to say that a_1 should start at least 3 units of time

before the start of a_2 and so on. To the best of our knowledge current extensions of GOLOG and HTN do not have such features. *Thus our main goal in this paper is to develop a language that allows the expression of domain knowledge* (*procedural and HTN-based*) of the above kind. We will refer to this language as Golog+HTN^{TI}, meaning that we add time and intervals to a language that has features from Golog and HTN.

To characterize Golog+HTN^{TI} we need an action theory that allows actions to have durations. For that we chose a simple extension of the language \mathcal{A} , which we refer to as \mathcal{AD} . We give the semantics of \mathcal{AD} using logic programming with answer sets. This (the semantics of \mathcal{AD}) allows us to define the notion of a trajectory. We use the notion of a trajectory to define the notion of a trace of a Golog+HTN^{TI} specification. We also use logic programming with answer sets (by adding additional rules to the logic program that defines a trajectory) to give an alternative definition of trace and show the two notions to be equivalent. Finally we try to show that using Golog+HTN^{TI} speeds up planning.

Background: LPASS and LP*smodels*

We now brie^{xy} introduce LPASS and its extension LP_{*smodels*}. An LPASS program is a collection of rules of the form

$$a_0 \leftarrow a_1, \ldots, a_m, \text{ not } a_{m+1}, \ldots, \text{ not } a_n$$
 (1)

where a_i 's are atoms. For an atom a, "not a" is referred to as a naf-literal. Intuitively, the above LPASS rule means that if $a_1 \ldots a_m$ are true and $a_{m+1} \ldots a_n$ can be assumed to be false then a_0 must be true.

The semantics of an LPASS program is defined using answer sets. LPASS programs whose rules do not have *not* in the body – referred to as definite programs – have unique answer sets, which are the least models of the theory obtained by treating rules of the form $a_0 \leftarrow a_1, \ldots, a_m$ as the classical formula $a_1 \land \ldots \land a_m \supset a_0$. Given an LPASS program P and a set of atoms S, the Gelfond-Lifschitz transformation P^S (Gelfond & Lifschitz 1990) is defined as the set of rules obtained from P by removing all rules from P whose body contains *not* b such that $b \in S$, and then removing the naf-literals from the rest of the rules. A set S of atoms is said to be an answer set of an LPASS program P if S is

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the answer set of the definite program P^S . Answer sets of propositional LPASS programs can be computed using answer set solvers such as smodels (Niemelä & Simons 1997) and dlv (Citrigno et al. 1997). By LP_{smodels} we refer to the extension of LPASS used in (Niemelä, Simons, & Soininen 1999) where rules of the following form are also allowed:

 $l\{b_1,\ldots,b_k\}u \leftarrow a_1,\ldots,a_m, not \ a_{m+1},\ldots,not \ a_n$ where a_i and b_j are atoms and l and u are two integers, and $l \leq u$. Intuitively, such a rule enforces the constraint that if the body is true then at least l and at most u atoms from the head are also true.

Reasoning about durative actions using LPASS

As we mentioned earlier, to characterize domain constraints, we need to £rst describe an action description language. The action description language that we plan to use is a simple extension of the language \mathcal{A} (Gelfond & Lifschitz 1998). In our extension, which we will refer to as \mathcal{AD} , we will allow actions to have duration and this will be sufficient to help us to justify and illustrate our language for domain constraints with new connectives.

Syntax of \mathcal{AD} . An action theory consists of two finite, disjoint sets of names A and F, called actions and ¤uents, respectively, and a set of propositions of the following form:

(2)causes(a, f)initially(f)(4)(3) executable $(a, \{p_1, \dots, p_n\})$ duration (a, v) (5) where f and p_i 's are puent literals (a puent literal is either a puent g or its negation $\neg g$) and a is an action. (2) is called a *dynamic causal law* and represents the effect of a while (3) states an executability condition of a. Intuitively, a proposition of the form (2) states that f is guaranteed to be true after the execution of a. An executability condition of a says that a is executable in a state in which p_1, \ldots, p_n hold. Propositions of the form (4) are used to describe the initial state. It

states that f holds in the initial state. Finally, a proposition of the form (5) is used to say that duration of action a is v. An action theory is a set of propositions of the form (2)-(5). We will assume that each action a appears in one and

only one proposition of the form (5) and v is a non-negative integer expression. We will often conveniently write d(a) to denote the value v if $duration(a, v) \in D$ and for a set of actions A, $d(A) = \max\{d(a) \mid a \in A\}$.

Example 1 Consider an action theory with the set of ¤uents $\{f, g, h\}$ and the set of actions $\{a, b, c, d\}$ and the following propositions:

causes(a, f)	duration(a, 3)	$executable(a, \{g, h\})$
causes(b, h)	duration(b, 2)	executable(b, {})
causes(c,g)	duration(c, 2)	$executable(c, \{\})$
$causes(d, \neg g)$	duration(d, 1)	$executable(d, \{\})$
initially $(\neg f)$	initially $(\neg g)$	initially $(\neg h)$

The propositions about a (the first line) say that a will cause the α units of time and is executable only if q and h are true. The propositions for other actions have similar meaning.

Since the characterization of \mathcal{AD} is not the aim of this paper, we do not present an independent characterization of it. (Recall that our goal is to use \mathcal{AD} to show how to plan using a proposed domain constraint language Golog+HTN TI .) Instead we give a LPASS encoding of prediction and planning using \mathcal{AD} . In another work, we present a transition function based characterization of \mathcal{AD} and prove that it is equivalent to the LPASS characterization in this paper.

Semantics: Prediction in \mathcal{AD} . Given a set of propositions D we construct an LPASS program $\pi_{\mathbf{D}}$ as follows:

1. For each v-proposition (4) in D, π_D contains the following rule: h(

$$(f,1). \tag{7}$$

This describes the initial state (which ¤uents hold in time point 1) as specified by the set of v-propositions in D.

2. For each ex-proposition (3) in D, π_D contains the following rules:

$$exec(a,T) \leftarrow not not_exec(a,T).$$
 (8)

$$ot_exec(a, I) \leftarrow not n(p_1, I).$$
 (9)

$$not_exec(a,T) \leftarrow not h(p_n,T).$$
 (10)

These rules define when a is executable at a time point T, based only on the truth of α uents. Rules (9)-(10) say that a is not executable if any of the ¤uent literals in its executability conditions does not hold.

3. For each d-proposition (5) in D, we add the following rules to π_D ,

$$ends(a, T+v) \leftarrow init(a, T).$$
 (11)

$$in_exec(a,T) \leftarrow init(a,T'), T' \leq T < T+v.$$
 (12)

These rules define when an action ends and when it is under execution.

4. For each action a and an ef-proposition (2), the following rules are added to π_D ,

$$h(f,T) \leftarrow ends(a,T).$$
 (13)

$$ab(f, T+1) \leftarrow init(a, T).$$
 (14)

These rules are used to reason about truth value of ¤uents at different time points.

Encoding the frame axiom. π_D contains the following rules that encode the frame axiom. They are slightly different from the normal LPASS encoding of the frame axiom so as to take into account action duration.

$$h(F,T+1) \leftarrow h(F,T), \text{ not } ab(\neg F,T+1).$$
 (15)

$$h(\neg F, T+1) \leftarrow h(\neg F, T), \text{ not } ab(F, T+1).$$
(16)

If we now want to £nd out if f would be true at time point tafter starting the execution of actions a_1 at time point t_1, a_2 at time point t_2, \ldots and a_n at time t_n all we need to do is to add

$$\{init(a_i, t_i) \mid i \in \{t_1, \dots, t_n\}\}$$

and the constraints

$$\leftarrow init(a_i, t_i), not \ exec(a_i, t_i)$$

(for i = 1, ..., n) to π_D , set the limits for the various variables, and ask if the resulting program entails h(f, t).

One assumption we made in our characterization is that we assume that the effect of an action takes into effect only after its execution ends, and the ¤uents, whose value changes due to an action execution, are in a unknown state during the execution. This of course can be changed by appropriately modifying π_D , in particular the rule (14).

Answer Set Planning with \mathcal{AD} Action Theories

We now show how the idea of answer set planning (Lifschitz 1999) can be extended to \mathcal{AD} action theories. Our LPASS planner for an action theory D, denoted by $\Pi(D)$, will consist of the program representing and reasoning about actions of D, π_D , the rules representing the goal, and the rules that generate action occurrences. Besides, we will need to set the limit on the maximal number of steps (the length) of the plan. We will call it *plan_size*. From now on, whenever we refer to a time point t, we mean that $1 \le t \le plan_size$.

Representing goal. Assume that we have a goal that is a conjunction of \exists uent literals $g_1 \land \ldots \land g_m$. We represent this by a set of atoms $\{finally(g_i) \mid i = 1, \ldots, m\}$. The following rules encode when the goal – as described by the *finally* facts – is satisfied at a time point T.

$$not_goal(T) \leftarrow finally(X), not h(X,T).$$
 (17)

$$goal(T) \leftarrow not not_goal(T).$$
 (18)

The following constraint eliminates otherwise possible answer sets where the goal is not satisfied at the time point *plan_size*.

$$\leftarrow not \ goal(plan_size). \tag{19}$$

We now de£ne the notion of a plan.

Definition 1 Given an action theory D, a goal G, and a plan size *plan_size*, we say that a sequence of sets of grounded actions A_1, \ldots, A_n is a *plan* achieving G if $goal(plan_size)$ is true in every answer set of the program the program $\pi^{PVer}(D, G)^1$, which consists of

- the rules of Π(D) in which the time variable is less than or equal *plan_size*;
- the rules representing G;
- the set of action occurrences

$$\bigcup_{i=1}^{n} \{ init(a,i) \mid a \in A_i \};$$

• the rules that disallow actions with contradictory conclusions to overlap (rules (23) and (24), below.

We say that a plan $p = A_1, \ldots, A_n$ is a concurrent plan if there exists a pair *i* and *j* and an action $a \in A_i \cap A_j$ such that i + d(a) > j, i.e., *p* contains an overlapping of two instantiations of a same actions. *p* is said to be *non*concurrent if it is not a concurrent plan.

Generating Action Occurrences. The following rules enumerate action initiations. To decrease the number of answer

sets we have made the assumption that two action instantiations corresponding to the same action can not overlap each other, i.e., we consider only non-concurrent plans. This need not be the case in general. Our point here is that LPASS allows us to express such restrictions very easily. For each action a with the duration v (i.e., **duration**(a, v) belongs to D), the following rule will be added to $\Pi(D)$:

$$\begin{array}{rcl} occ_before(a,T) &\leftarrow & init(a,T_1),T_1 < T < T_1 + v. & (20) \\ & init(a,T) &\leftarrow & exec(a,T), & (21) \\ & & & not \ occ_before(a,T), \\ & & & not \ oct_init(a,T). \\ & & not \ init(a,T). & (22) \end{array}$$

The next rules disallow actions with contradictory effects to overlap: for every pair of a and b such that **causes**(a, f) and **causes** $(b, \neg f)$ belong to D, Π_D contains the two rules:

$$overlap(a, b, T) \leftarrow in_exec(a, T), in_exec(b, T).$$
 (23)
 $\leftarrow overlap(a, b, T).$ (24)

Let $\pi^{PGen}(D,G)$ be the set of rules of $\Pi(D)$ with the goal G and $plan_size=n$. For an answer set M of $\pi^{PGen}(D,G)$, let $s_i(M) = \{f \mid h(f,i) \in M\}$ and $A_i(M) = \{a \mid init(a,i) \in M\}$. We can prove that

Theorem 1 For an action theory D and a goal G, B_1, \ldots, B_n is a non-concurrent plan that achieves G iff there exists an answer set M of $\pi^{PGen}(D, G)$ such that $A_i(M) = B_i$.

Golog+HTN^{TI}: Using durations in Procedural and Hierarchical domain Constraints

We begin with an informal discussion on the new construct in Golog+HTN^{TI}. Consider the domain from Example 1. It is easy to see that the program b; c; a is a plan achieving ffrom any state and the time needed to execute this plan is the sum of the actions's durations (Figure 1, Case (a)). Observe that b and c are two actions that achieve the condition for a to be executable and can be executed in parallel. Hence it should be obvious that any plan that allows b and c to execute in parallel will have a shorter execution time. For the moment, let us represent this by the program $p_1 = \{b, c\}; a$. The execution of this program is depicted in Figure 1, Case (b).



Figure 1: A pictorial view of program execution (the dot shows when an action starts and the arrow shows when an action stops)

Now consider a modification of the domain in Example 1, in which the executable propositions of c changes to **executable** $(c, \{\neg g\})$. A program achieving f would be to execute b and d in parallel, then c, and lastly a. We cannot execute b, c, and d in parallel all the time because c is not

¹The ^{PVer} stands for *plan verification*.

executable until $\neg g$ holds, and hence, it might need to wait for d to £nish. It is easy to see, however, that it is better if cstarts whenever d £nishes. To account for this, we introduce a new construct that allows programs to start even if the preceding program has not £nished. We write $(\{b, d\}; _{[1,1]}^s c); a$ to indicate that c should start its execution 1 time unit after $\{b, d\}$ and then a and denote this program by p_2 . The execution of this program can be illustrated as follows.

$$\begin{array}{c} \bullet & \bullet \\ \bullet & \bullet \\ \bullet & \bullet \\ \bullet & \bullet \\ \hline 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 \\ \hline & & & & & \\ \bullet & & & & \\ \hline \end{array}$$

Figure 2: Execution of $(\{b, d\};_{[1,1]}^{s} c); a$

We now define programs in $Golog+HTN^{TI}$ that express domain knowledge to be exploited by a planner.

De£nition 2 (Program) For an action theory *D*,

- 1. an action *a* is a program;
- 2. a temporal constraint $\phi[t_1, t_2]$ is a program;
- 3. if p_1 and p_2 are programs and $0 \le t_1 \le t_2$ are two time non-negative integers then so are $(p_1|p_2)$, $(p_1;_{[t_1,t_2]}^s p_2)$, and $(p_1;_{[t_1,t_2]}^e p_2)$;
- 4. if p_1 and p_2 are programs and ϕ is a ¤uent formula then so are "if ϕ then p_1 else p_2 " and "while ϕ do p";
- 5. if X_1, \ldots, X_n are variables of sort s_1, \ldots, s_n , respectively, $p(X_1, \ldots, X_n)$ is a program, and $f(X_1, \ldots, X_n)$ is a formula, then **pick** $(\vec{X}, f(\vec{X}), p(\vec{X}))$ is a program where \vec{X} stands for X_1, \ldots, X_n ;
- 6. if p_1, \ldots, p_n are programs then a pair (S, C) is a program where $S = \{p_1, \ldots, p_n\}$ and C is a set of constraints over S of the following form:

i) $p_1 \prec_{[t_1,t_2]}^s p_2$ (or $p_1 \prec_{[t_1,t_2]}^e p_2$), (ii) $(p,\phi[t_1,t_2])$, (iii) $(\phi[t_1,t_2],p)$, and (iv) $(p_1,\phi[t_1,t_2],p_2)$ where p,p_1,p_2 are programs, ϕ is a ¤uent formula and $0 \le t_1 \le t_2$.

The constructs 1-5 in the above de£nitions are generalizations of constructs in GOLOG (Levesque *et al.* 1997) and the construct 6 is a generalization of hierarchical task networks (HTN) (Erol, Nau, & Subrahmanian 1995).

Intuitively, $\phi[t_1, t_2]$ expresses the constraint that ϕ holds during the time interval $[t_1, t_2]$ (from the current moment) and $(p_1;_{[t_1,t_2]}^s p_2)$ states that p_2 should start its execution at least t_1 and at most t_2 units of time after p_1 starts whereas $(p_1;_{[t_1,t_2]}^e p_2)$ forces p_2 to wait for t ($t_1 \leq t \leq t_2$) units of time after p_1 finishes. It is easy to see that $(p_1;_{[0,0]}^s p_2)$ requires that p_1 and p_2 be executed in parallel whereas $(p_1;_{[0,0]}^e p_2)$ requires that p_2 starts its execution at the time p_1 finishes. Note that $(p_1;_{[0,0]}^e p_2)$ corresponds to the original notation $p_1; p_2$.

The constraints in item 6 above are similar to truth constraints and ordering constraints over tasks in HTN. Intuitively, $p_1 \prec_{[t_1,t_2]}^s$ says that p_2 can start its execution after p_1 is in execution (or after p_1 £nishes its execution) for t_1 time units but no later than t_2 time units of time. Similarly, $(p, \phi[t_1, t_2])$ (resp. $(\phi[t_1, t_2], p))$ means that ϕ must hold from t_1 to t_2 immediately after (resp. before) p's execution. $(p_1, \phi[t_1, t_2], p_2)$ states that p_1 must start before p_2 and ϕ must hold t_1 units of time after p_1 starts until t_2 units of time before p_2 starts.

Example 2 In our notation, p_1 and p_2 (from the discussion before Figure 1) are represented by $((b;_{[0,0]}^s c);_{[0,0]}^e a)$ and $(((b;_{[0,0]}^s d);_{[1,1]}^s c);_{[0,0]}^e a)$, respectively.

We will now define the notion of a trace of a program, which describe what actions are done when. But first we need to define the notion of a trajectory. For an action theory D and an integer n, let $\pi^{Gen}(D)$ be the program consisting of the set of rules of $\Pi(D)$ whose time variable belongs to the set $1, \ldots, n$ (recall that $\Pi(D)$ consists of the rules (7)-(16) and (20)-(24)).

Definition 3 (Trajectory) For an action theory D and an answer set M of $\pi^{PGen}(D)$, let $s_i = \{f \mid h(f,i) \in M\}$ and $A_i = \{a \mid init(a,i) \in M\}$. We say that the sequence $\alpha = s_1A_1 \dots s_nA_n$ is a *trajectory* of D.

Intuitively, a trajectory is an alternating sequence of states and action occurrences s_1A_1, \ldots, s_nA_n , where s_i is a state at time point *i* and A_i is the set of actions that are supposed to have occurred at time point *i*. We are now ready to de£ne what is a trace of a program. Since the de£nition of a trace is somewhat complicated we divide it into several small de£nitions and illustrate the complex ones with examples. First, we begin with the primitive cases.

Definition 4 (Trace - Primitive Cases) A trajectory $\alpha = s_1 A_1 \dots s_n A_n$ is a trace of a program p if

• p = a, n = d(a) and $A_1 = \{a\}$ and $A_i = \emptyset$ for i > 1; or • $p = \phi[t_1, t_2], n = t_2, A_i = \emptyset$ for every i, and ϕ holds in s_t for $t_1 \le t \le t_2$.

The next definition deals with programs that are constructed using GOLOG-constructs ((Levesque *et al.* 1997)).

Definition 5 (Trace – Programs with GOLOG-Constructs) A trajectory $\alpha = s_1A_1 \dots s_nA_n$ is a trace of a program p if one of the following is satisfied.

• $p = p_1 \mid p_2, \alpha$ is a trace of p_1 or α is a trace of p_2 ,

• $p = \text{if } \phi$ then p_1 else p_2 , α is a trace of p_1 and ϕ holds in s_1 or α is a trace of p_2 and $\neg \phi$ holds in s_1 ,

• p = while ϕ do p_1 , n = 1 and $\neg \phi$ holds in s_1 or ϕ holds in s_1 and there exists some *i* such that $s_1A_1 \dots A_i$ is a trace of p_1 and $s_{i+1}A_{i+1} \dots A_n$ is a trace of *p*, or

• $p = \mathbf{pick}(\vec{X}, f(\vec{X}), q(\vec{X}))$, then there exists a constant \vec{x} of the sort of \vec{X} such that $f(\vec{x})$ holds in s_1 and α is a trace of $q(\vec{x})$.

The trace of each program is defined based on its structure, i.e., how it is built. We next deal with the new connectives $;_{[t_1,t_2]}^s$ and $;_{[t_1,t_2]}^e$.

Definition 6 (Trace – Parallel and Overlapping Programs) A trajectory $\alpha = s_1 A_1 \dots s_n A_n$ is a trace of a program p if

• $p=p_1$; $_{[t_1,t_2]}^s p_2$, there exists two numbers t_3 and t_4 such that $t_1 + 1 \le t_3 \le t_2 + 1$ and $t_4 \le n$ (because the index of the trace starts from 1) and either (i) there exists a trace $s_1B_1 \dots s_{t_4}B_{t_4}$ of p_1 and a trace $s_{t_3}C_{t_3} \dots s_nC_n$ of p_2 such

that $A_i = B_i \cup C_i$ for every i; or (ii) $t_3 \le t_4$ and there exists a trace $s_1 B_1 \dots s_n B_n$ of p_1 and a trace $s_{t_3} C_{t_3} \dots s_{t_4} C_{t_4}$ of p_2 such that $A_i = B_i \cup C_i$ (we write $B_j = \emptyset$ or $C_j = \emptyset$ for indexes that do not belong to the trace of p_1 or p_2); or

• $p=p_1;_{[t_1,t_2]}^e p_2$, there exists two numbers t_3 and t_4 such that $t_1 + t_3 \le t_4 \le t_2 + t_3$ and $t_4 \le n$ and $s_1A_1 \dots s_{t_3}A_{t_3}$ is a trace of p_1 and a trace $s_{t_4}A_{t_4} \dots s_nA_n$ is a trace of p_2 and $A_i = \emptyset$ for every $t_3 \le i < t_4$.

This definition is best illustrated using a picture.

Figure 3: $A_i = B_i \cup C_i$ – First Item, Case 1 (De£nition 6)

Example 3 • For $p_1 = ((b;_{[0,0]}^s c);_{[0,0]}^e a)$ (wrt. the action theory in Example 1), we can easily check that

$$\mathbf{s_1^1} \left\{ \mathbf{b}, \mathbf{c} \right\} \mathbf{s_2^1} \emptyset \ \mathbf{s_3^1} \left\{ \mathbf{a} \right\} \mathbf{s_4^1} \emptyset \ \mathbf{s_5^1} \emptyset \ \mathbf{s_6^1} \emptyset$$

where

$$- s_{1}^{1} = \{\neg f, \neg g, \neg h\}, \\ - s_{2}^{1} = \{\neg f\}, \\ - s_{3}^{1} = \{\neg f, g, h\}, \\ - s_{4}^{1} = \{g, h\}, \\ - s_{5}^{1} = \{g, h\}, \\ - s_{6}^{1} = \{f, g, h\}, \\ - s_{6}^{1} = \{f, g, h\}, \\ \text{is a trace of } p_{1}. \text{ On the other}$$

is a trace of p_1 . On the other hand,

$$\mathbf{s}_{1}^{1} \left\{ \mathbf{b}, \mathbf{c}, \mathbf{d} \right\} \mathbf{s}_{2}^{1} \emptyset \mathbf{s}_{3}^{1} \left\{ \mathbf{a} \right\} \mathbf{s}_{4}^{1} \emptyset \mathbf{s}_{5}^{1} \emptyset \mathbf{s}_{6}^{1} \emptyset$$

although it contains a trace of p_1 .

• For $p_2 = (((b;_{[0,0]}^s d);_{[1,1]}^s c);_{[0,0]}^e a)$. (wrt. the modified action theory), we can easily check that

 $s_1^2 \ \{b,d\} \ s_2^2 \ \{c\} \ s_3^2 \ \emptyset \ s_4^2 \{a\} \ s_5^2 \ \emptyset \ s_6^2 \ \emptyset \ s_7^2 \ \emptyset$

where

 $\begin{array}{l} - \ s_1^2 = \{\neg f, \neg g, \neg h\}, \\ - \ s_2^2 = \{\neg f, \neg g\}, \\ - \ s_3^2 = \{\neg f, h\}, \\ - \ s_4^2 = \{\neg f, g, h\}, \\ - \ s_5^2 = \{g, h\}, \\ - \ s_6^2 = \{g, h\}, \\ - \ s_7^2 = \{f, g, h\}, \end{array}$

is a trace of p_2 . but

 $s_{1}^{2}\left\{ b,d\right\} s_{2}^{2} \, \emptyset \, s_{2}^{2} \left\{ c\right\} s_{3}^{2} \, \emptyset \, s_{4}^{2} \{a\} \, s_{5}^{2} \, \emptyset \, s_{6}^{2} \, \emptyset \, s_{7}^{2} \, \emptyset$

is not a trace of p_2 because c should start at the time moment 2.

In the next definition we deal with HTN-programs.

Definition 7 (Trace - HTN Programs) A trajectory $\alpha = s_1A_1 \dots s_nA_n$ is a trace of a program p = (S,C) with $S = \{p_1, \dots, p_k\}$ if there exists two sequences of numbers b_1, \dots, b_k and e_1, \dots, e_k with $b_j \leq e_j$, a permutation (i_1, \dots, i_k) of $(1, \dots, k)$, and a sequence of traces

 $\alpha_j = s_{b_j} A_{b_j}^j \dots s_{e_j} A_{e_j}^j$ that satisfy the following conditions:

- for each $l, 1 \leq l \leq k, \alpha_l$ is a trace of p_{i_l} ,
- if $p_t \prec p_l \in C$ then $i_t < i_l$,
- if $p_t \prec_{[q_1,q_2]}^s p_l \in C$ then $i_t < i_l$ and $b_{i_t} + q_1 \leq b_{i_l} \leq b_{i_t} + q_2$,

• if $p_t \prec_{[q_1,q_2]}^e p_l \in C$ then $i_t < i_l$ and $e_{i_t} + q_1 \le b_{i_l} \le e_{i_t} + q_2$,

• if $(\phi[t_1, t_2], p_l) \in C$ (or $(p_l, \phi[t_1, t_2]) \in C$) then ϕ holds in the state $s_{b_{i_l}-t_2}, \ldots, s_{b_{i_l}-t_1}$ (or $s_{e_{i_l}+t_1}, \ldots, s_{e_{i_l}+t_2}$), and • if $(p_t, \phi[t_1, t_2], p_l) \in C$ then ϕ holds in $s_{b_{i_t}+t_1}, \ldots, s_{b_{i_l}-t_2}$.

• $A_i = \bigcup_{j=1}^k A_i^j$ for every i = 1, ..., n where we assume that $A_i^j = \emptyset$ for $i < b_j$ or $i > e_j$.

The intuition of the above definition is as follows. First, each program starts $(b_i$'s) and ends $(e_i$'s) at some time point and it cannot finish before it even starts, hence, the requirement $b_i \leq e_i$. The order of the execution is specified by the ordering constraints and not by the program's number. The permutation (i_1, \ldots, i_k) and j's record the starting time of the programs. The conditions on the trajectories make sure that the constraints are satisfied (first four items) and they indeed create A_1, \ldots, A_n (last item).

An LPASS interpreter

We now present an LPASS interpreter for programs. We will adopt the way to encode formulas and programs in (Son, Baral, & McIIraith 2001) for use with answer set solvers. In short, each program p (resp. formula ϕ) will be associated with a unique name n_p (resp. n_{ϕ}) and will be replaced by a set of rules and facts, denoted by $r(n_p)$ (resp. $r(n_{\phi})$). The formal definition of $r(n_p)$ and $r(n_{\phi})$ can be found in the aforementioned paper. Here, we demonstrate it by an example.

Example 4 $p_1 = ((b;_{[0,0]}^s c);_{[0,0]}^e a)$ is encoded by the two atoms $proc(p_1, p_1^1, a, start, 0, 0)$ and $proc(p_1^1, b, c, start, 0, 0)$.

 $\begin{array}{l} p_2{=}(((b;_{[0,0]}^sd);_{[1,1]}^sc);_{[0,0]}^ea) \ \text{is encoded by the atoms} \\ proc(p_2,p_2^1,a,end,0,0), \ proc(p_2^1,p_2^2,c,start,1,1), \ \text{and} \\ proc(p_2^2,b,c,start,0,0). \end{array}$

In the above, a program is specified by the predicate *proc* with 5 arguments: the name, the first sub-program (the head), the rest of the program (the tail), whether the tail should start relative to the start or to the end of the head (*start/end*), and the minimal or the maximal time the tail needs to wait. Programs constructed using other constructs are encoded similarly. For example, the program $p = \mathbf{if} \phi$ then p_1 else p_2 is encoded by the atom $if(p, n_{\phi}, p_1, p_2)$ and the set of atoms encoding p_1 and p_2 , and $\phi[t_1, t_2]$ by $formula(n_{\phi}, t_1, t_2)$ etc.

For a program p of an action theory D, we define a logic program II that consists of the rules encoding the domain, π_D , the rules describing the program $r(n_p)$, the set of rules for generating action occurrences (20)-(24), and a set of rules that realizes the operational semantics of programs. We follow the approach in (Son, Baral, & McIlraith 2001) and define a predicate $trans(p, t_1, t_2)$ which holds in an answer set M iff $s_{t_1}(M)A_{t_1}(M)\ldots s_{t_2}(M)A_{t_2}(M)$ is a trace of p^2 . We will concentrate on describing the ideas behind the rules and their meaning rather than presenting the rules in great detail. We will present only a few representative rules. Readers interested in the source code of the program can obtain it from our web site³.

We will begin with an informal discussion on the ideas behind the rules defining $trans(p, t_1, t_2)$. Intuitively, because of the rules (20)-(24), each answer set M of the program II will contain a sequence of sets of actions $\alpha = A_1, \ldots, A_n$ where $A_i = \{a \mid init(a, i) \in M\}$. The encoding of the action theory, π_D , makes sure that whenever an action a is initiated it is executable. Thus, the sequence α is a trajectory of D. So, it remains to be verified that α is indeed a trace of the program p. We will do this in two steps. First, we check if α contains a trace of p, i.e., we make sure that there is a trace $s_1B_1 \ldots s_nB_n$ of p such that $B_i \subseteq A_i$. Second, we make sure that no action is initiated when it is not needed. To do so, we define two predicates:

• $tr(p, t_1, t_2)$ - $s_{t_1}A_{t_1} \dots A_{t_2}$ contains a trace of p;

• $used_in(p, q, t, t_1, t_2)$ - a trace of p starting from t is used in constructing a trace of q from t_1 to t_2 . Intuitively, this predicate records the actions belonging to the traces of q. The de£nition of this predicate will make sure that for a simple action a, only action a is used to construct its trace, i.e., $used_in(a, a, t_1, t_1, t_1 + d(a))$ is equivalent to $init(a, t_1)$ and $used_in(b, a, t_1, t_1, t_1 + d(a))$ is false for every $b \neq a$.

Finally, we say that $trans(p, t_1, t_2)$ holds iff $tr(p, t_1, t_2)$ holds and every action $a \in A_j$ for $t_1 \leq j \leq t_2$, $used_in(a, p, j, t_1, t_2)$ holds. The rules for $tr(p, t_1, t_2)$ are similar to the rules of the predicate $trans(p, t_1, t_2)$ from (Son, Baral, & McIIraith 2001) with changes that account for action duration and the new constructs such as $;^s_{[t_1,t_2]}$ and $;^e_{[t_1,t_2]}$ and checking for the condition of new constraint on a HTN-program. Below, we list some of the rules for tr.

$$\begin{aligned} tr(A, T_1, T_1 + D) &\leftarrow & init(A, T_1), duration(A, D). \end{aligned} (25) \\ tr(P, T_1, T_2) &\leftarrow & proc(P, P_1, P_2, start, M_1, M_2), \end{aligned} (26) \\ &T_1 + M_1 \leq T_3 \leq T_1 + M_2, \\ &T_1 \leq T_4 \leq T_2, \end{aligned}$$

$$tr(P, T_1, T_2) \leftarrow tr(P_1, T_1, T_4), tr(P_2, T_3, T_2).$$

$$tr(P, T_1, T_2) \leftarrow proc(P, P_1, P_2, start, M_1, M_2), (27)$$

$$T_1 + M_1 \leq T_3 \leq T_1 + M_2,$$

$$T_3 \leq T_4 \leq T_2,$$

$$tr(P_1, T_1, T_2), tr(P_2, T_3, T_4).$$

$$tr(P, T_1, T_2) \leftarrow proc(P, P_1, P_2, end, M_1, M_2), (28)$$

$$T_3 \leq T_4, T_3 + M_1 \leq T_4 \leq T_3 + M_2,$$

$$tr(P_1, T_1, T_3), tr(P_2, T_4, T_2).$$

$$tr(I, T_1, T_2) \leftarrow if(I, F, P_1, P_2),$$

$$hf(F, T_1), tr(P_1, T_1, T_2).$$
(29)

$$tr(I, T_1, T_2) \leftarrow if(I, F, P_1, P_2),$$
 (30)
not $hf(F, T_1), tr(P_2, T_1, T_2).^4$

²For an answer set M, $s_i(M) = \{f \mid h(f,i) \in M, f \text{ is a } uent literal\}$ and $A_i(M) = \{a \mid init(a,i) \in M\}$.

We next present the rules defining tr for HTN-programs. First, we begin with the encoding of a HTN-program. A program p = (S, C) is encoded by the set of atoms and rules encoding S and C where elements of C will be represented by the predicates

- $order(*, +, +, start, m_1, m_2)$,
- $order(*, +, +, end, m_1, m_2)$,
- $postC(*, +, -, m_1, m_2)$,
- $preC(*, -, +, m_1, m_2)$, and
- $maintain(*, +, -, +, m_1, m_2)$

where m_1 , m_2 are non-negative integers representing units of time and the place holder '*', '+', or '-' denotes the name of the constraint, a program, or a formula, respectively. To make sure that for every program q belonging to p, the trajectory $s_{t_1}A_{t_1} \ldots A_{t_2}$ contains a trace of q, we generate the begin- and end-point of each q, denoted by $begin(p, q, t_{q_1})$ and $end(p, q, t_{q_2})$, respectively, and then check whether $tr(q, t_{q_1}, t_{q_2})$ holds or not. The key idea is to check whether this creates a trace for p. For this reason, we define a predicate on trace(p, t) and $nok(p, t_1, t_2)$ to say that the trace of p contains the time moment t and the current assignment of start- and end-point for the programs belonging to S does not satisfy the constraints in C. Some of these rules are given below:

$$nok(N, T_1, T_2) \leftarrow htn(N, S, C), T_1 \leq T \leq T_2,$$
 (31)
 $not \ on_trace(N, T).$

The first rule says that every time point between T_1 and T_2 must be on the trace of p. The second checks for the ordering constraints in C. Rules to check for truth constraints are to the second rule and are omitted here.

We now define the rules for $used in(p, q, t, t_1, t_2)$. We have the following rules.

$$used_in(A, A, T_1, T_1, T_2) \leftarrow action(A), tr(A, T_1, T_2).$$
(33)
$$used_in(P, Q, T_3, T_1, T_2) \leftarrow T_1 \leq T_3 \leq T_2,$$
(34)
$$T_4 \leq T_2, T_1 \leq T_5 \leq T_2,$$

$$T_4 \leq T_3 \leq T_5,$$

$$used_in(P, Q_1, T_3, T_4, T_5),$$

$$used_in(Q_1, Q, T_4, T_1, T_2).$$

The first rule accounts for the fact that $used_in(a, a, t, t, t + d(a))$ is always true if init(a, t) is true. The second rule says that if p is used in a trace of q_1 and q_1 is in a trace of q then p is also in a trace of q. These two rules are not enough, however, because so far we have not specified when a program

³http://www.cs.nmsu.edu/~tson/duration.

⁴Rules for tr to work with other programs such as the while-do or non-deterministic choice of arguments **pick** or actions | are defined similarly. We must note that in defining tr using the rules for trans given in (Son, Baral, & McIlraith 2001), we have improved them in several aspects. The style is similar though.

p is used in a trace of q. This is done easily by using the weight rules. For instance, instead of the rule (26), we use the following rule:

$$\begin{aligned} &\{tr(P, T_1, T_2), used_in(P_1, P, T_1, T_1, T_2), \\ &used_in(P_2, P, T_3, T_1, T_2)\}3 \leftarrow \\ &proc(P, P_1, P_2, start, M_1, M_2), \\ &T_1 + M_1 \leq T_3 \leq T_1 + M_2, T_1 \leq T_4 \leq T_2, \\ &tr(P_1, T_1, T_4), tr(P_2, T_3, T_2). \end{aligned}$$

$$(26')$$

The intuition of the above rule is that whenever we used the rule to derive $tr(P, T_1, T_2)$ then we also record what sub-programs are used and starting from which moment (by requiring that $used_in(P_1, P, T_1, T_1, T_2)$ and $used_in(P_2, P, T_3, T_1, T_2)$ also true). Similarly modification needs to be done for other rules defining tr. We omit them here for space reason.

Having defined tr and $used_in$, defining trans is simple: for every program P, $trans(P, T_1, T_2)$ holds only if $tr(P, T_1, T_2)$ holds and every action A initiated during T_1 and $T_2 - 1$ must be used to construct a trace of P from T_1 to T_2 . So, we have the following rules:

$$not_min(P,T_1,T_2) \leftarrow action(A), init(A,T), \quad (35)$$

$$T_1 \leq T \leq T_2,$$

$$not \ used_in(A,P,T,T_1,T_2).$$

$$trans(P,T_1,T_2) \leftarrow T_1 \leq T_2, tr(P,T_1,T_2), \quad (36)$$

$$not \ not_min(P,T_1,T_2).$$

We illustrate this definition using a simple example.

Example 5 Consider $p_1 = ((b_{[0,0]}^s c);_{[0,0]}^e a)$ from Example 4 and the trajectory $\{b, c\}, \emptyset, \{a\}, \emptyset, \emptyset, \emptyset$.

For $p_1 = ((b_{[0,0]}^s c);_{[0,0]}^e a)$ (wrt. the action theory in Example 1) from Example 4 and the trajectory (Example 3)

$$\mathbf{s_1^1} \{ \mathbf{b}, \mathbf{c} \} \mathbf{s_2^1} \emptyset \mathbf{s_3^1} \{ \mathbf{a} \} \mathbf{s_4^1} \emptyset \mathbf{s_5^1} \emptyset \mathbf{s_6^1} \emptyset$$

with

• $s_1^1 = \{\neg f, \neg g, \neg h\},\$

•
$$s_2^1 = \{\neg f\},\$$

•
$$s_3^1 = \{\neg f, g, h\},\$$

•
$$s_4^1 = \{g, h\},$$

• $s_5^1 = \{g, h\},$

•
$$s_6^1 = \{f, g, h\}.$$

Clearly, tr(b, 1, 3), tr(c, 1, 3), tr(a, 3, 6) hold (because of rule (25)). $used_in(b, b, 1, 1, 3)$, $used_in(c, c, 1, 1, 3)$, and $used_in(a, a, 3, 3, 6)$ hold (because of rule (33)). Furthermore, we have $tr(p_1^1, 1, 3)$, $used_in(b, p_1^1, 1, 1, 3)$ and $used_in(c, p_1^1, 1, 1, 3)$ hold (because of (26')). Similarly, $tr(p_1, 1, 6)$, $used_in(b, p_1, 1, 1, 6)$, $used_in(c, p_1, 1, 1, 6)$, and $used_in(a, p_1, 3, 1, 6)$ hold (because of (26') and (34)). This implies that $trans(p_1, 1, 6)$ holds. It is worth noting that trans(b, 1, 3) does not hold since c is initiated at 1 but $used_in(c, b, 1, 1, 3)$ does not hold.

We next present a theorem that extends a result from (Son, Baral, & McIlraith 2001) discussing a property of the above described program. Let p be a program and D be an action theory. Let Π_n be the program consisting of

• the set of rules of $\Pi(D)$,

- the rules defining tr, used in, and trans, and
- the rule expressing our goal of £nding a trace of p

$$\leftarrow not \ trans(p, 1, n)$$

where all the time variables in Π_n are bounded by n. Extending a result from (Son, Baral, & McIlraith 2001), we have the following theorem.

Theorem 2 For an action theory D and a program p, (i) for every answer set M of Π_n , $s_1(M)A_1 \dots s_n(M)A_n(M)$ is a trace of p; and (ii) if $s_1B_1s_2 \dots s_nB_n$ is a trace of p then there exists an answer set M of Π_n such that $s_i = \{f \mid h(f,i) \in M\}$ and $B_i = \{a \mid init(a,i) \in M\}$.

Experimental Evaluations

We have used Golog+HTN^{T1} in planning for domains from the AIPS2002 competition. We concentrate on formulating and testing our language in complex domains in which actions have durations, which might depend on the concrete situation. For example, the duration of £lling a tank depends on various factors: the current level of fuel in the tank, the rate of which the fuel ¤ows, etc. Of the 13 planners competed in the AIPS2002 competition, only 5 have this capability (see (Long *et al.*)). As an example, our planner ⁵ can solve *all* 20 Zeno Flying problems in which the £rst seven problems were solved in less than 1 second, the next six problems were solved within 10 to 60 seconds.

Conclusion

In this paper we proposed a domain constraint lan-guage $Golog+HTN^{TI}$ that generalizes procedural (based on GOLOG) and HTN-based domain constraints to allow time intervals. In the process we generalize the connective ';' to two connectives $;_{[t_1,t_2]}^s$ and $;_{[t_1,t_2]}^e$ and similar generalizations of HTN constraints. We then show how the answer set planning paradigm can be used to plan where actions have duration, and we have domain constraints expressed in the language $Golog+HTN^{TI}$. In terms of related work (that we have not mentioned yet) Reiter in (Reiter 2001) discusses temporal GOLOG where time is a parameter of the actions. Two differences (as relevant to the focus of this paper) between his approach and ours is that we generalize the connective ';' rather than actions, and we consider HTN-based constructs not considered by Reiter. Other differences include his use of Situation calculus (and £rst-order logic) as opposed to our use of a propositional action theory. cc-Golog (Grosskreutz & Lakemeyer 2000) extended Con-Golog to allow time to be added to the program but cc-Golog concentrates on accommodating even-driven behavior rather than for planning.

⁵We contacted authors of other planners to help us setting up their planners so that a fair comparison between our planner and theirs can be done. Unfortunately, we were not able to £nish this task in a timely fashion and did not yet have the comparison ready for this paper. We plan to have this issue resolved as soon as possible.

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